

REGLA DE CALCULO

SEXTON'S OMNIMETRE

La escala VERSED SINES



**Gonzalo Martin**  
**Julio 2012**

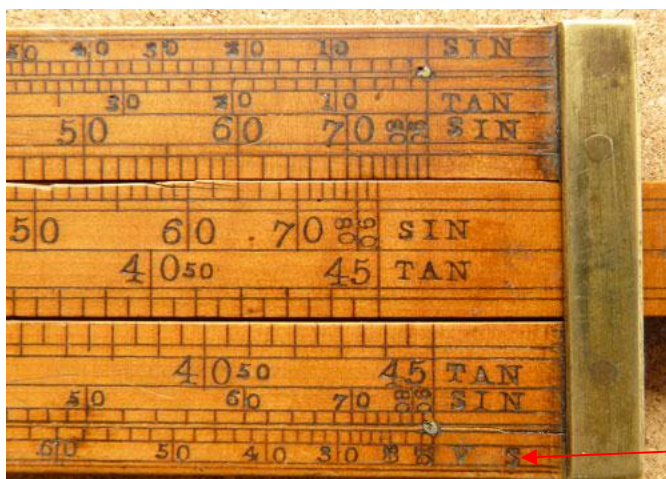
La escala 'versed sines' (**v.s.**) de la regla Omnimetre representa exactamente la función trigonométrica del mismo nombre y cuyo valor es  $vs(a) = 1 - \cos(a)$ .

Esta escala se encuentra raramente en las reglas de cálculo salvo en las reglas antiguas llamadas de Gunter, pero en este caso el significado de la escala **V.S** es diferente, como veremos mas adelante.

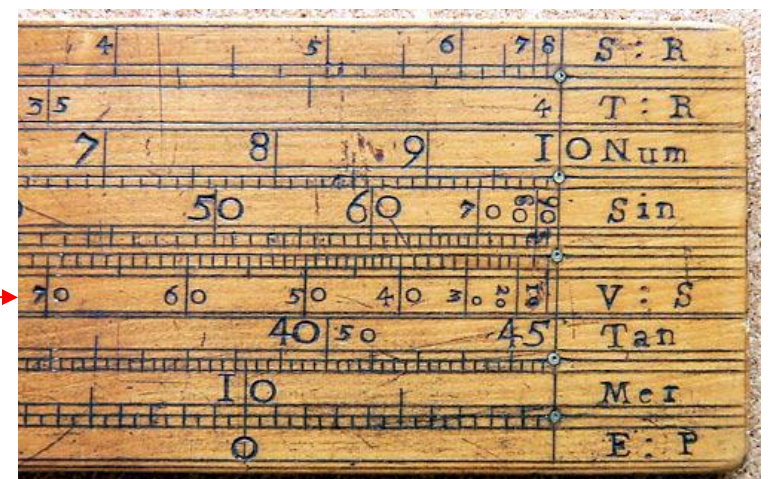
Hemos comparado diferentes valores de v.s., obtenidos directamente en la regla, con los valores determinados por una tabla de 'Natural Versed Sines' , los valores de la regla son correctos, se tratan bien de '**versed sines**'

No se ha encontrado ningún ejemplo de utilización de la escala **V.S** en los tratados antiguos de navegación disponibles sur Internet. En la última página dos grandes coleccionistas explican que el valor de esta escala sería « 1-haversine »

### Escala V.S en una Plain Scale Gunter



### Escala V.S en una regla Gunter

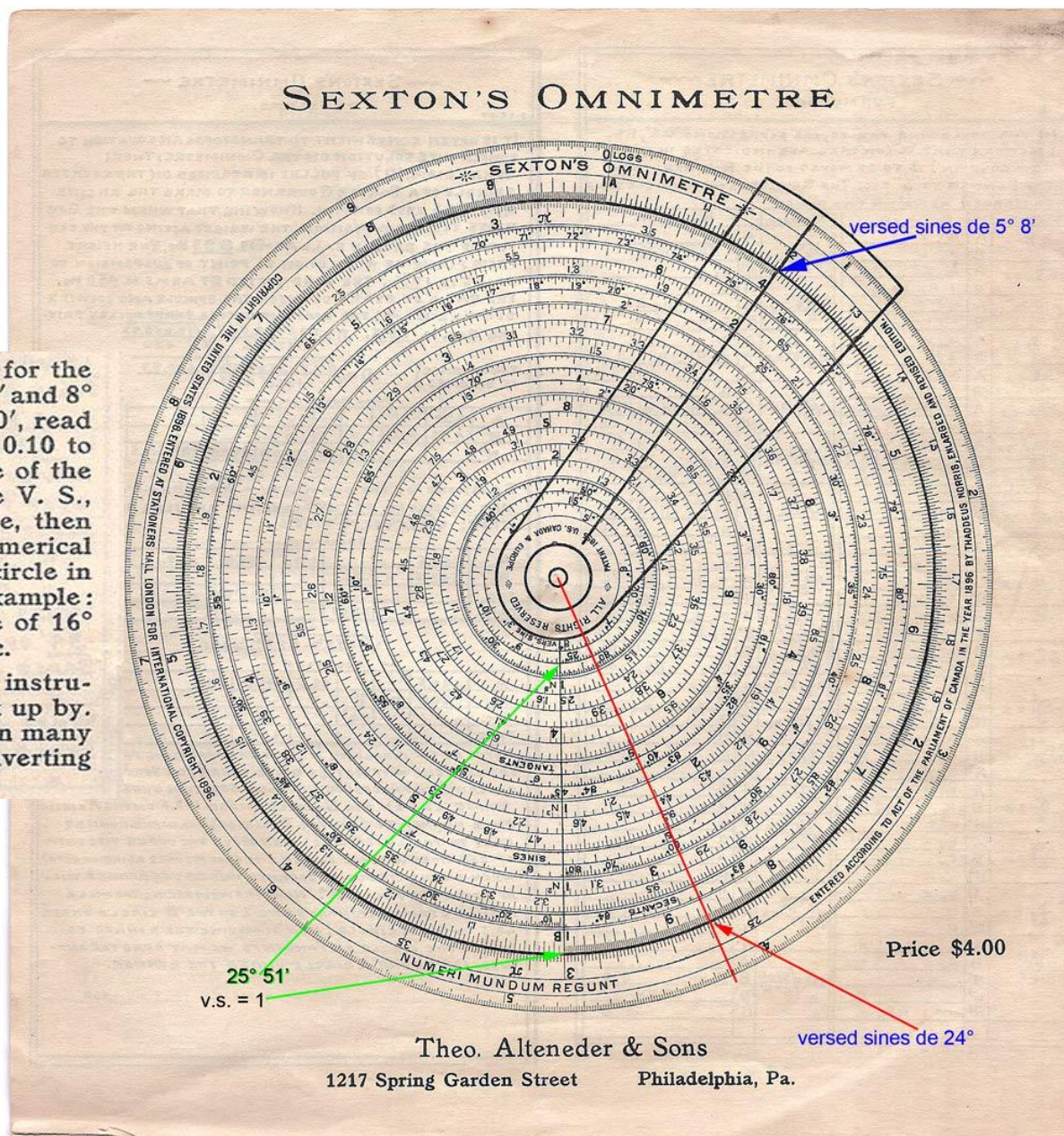


### Escala V.S en una Sliding Gunter

Valores de diferentes versed sines encontrados con el Sexton's Omnimetre

V. S. Scale of VERSED SINES, to be read on scale B for the angle shown on V. S. If the angle be between  $2^{\circ} 35'$  and  $8^{\circ} 5'$ , read 0.001 to 0.010. If between  $8^{\circ} 5'$  and  $25^{\circ} 50'$ , read 0.010 to 0.100. If between  $25^{\circ} 50'$  and  $90^{\circ}$ , read 0.10 to 1.00. This means that to find the numerical value of the versed sine of any angle, find the angle on scale V. S., bring the runner over it, hold the runner in place, then look on scale B, and under the runner read its numerical value, placing the decimal point according to the circle in which the angle is found, as defined above. Example: The versed sine of  $5^{\circ} 8' = 0.004$ . The versed sine of  $16^{\circ} 16' = 0.040$ . The versed sine of  $53^{\circ} 8' = 0.400$ , etc.

The Clamp-screw is not designed to turn any part of the instrument, but simply to serve as a pivot and to pick it up by. It is also used to clamp the two discs together when many readings are to be taken from one setting, as in converting cubic feet to gallons, inches to millimetres, etc.



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London:

PRINTED FOR THE AUTHOR,

AND SOLD BY CHARLES WILSON, LATE J. W. NORIE & WILSON,

AT THE NAVIGATION WAREHOUSE AND NAVAL ACADEMY,

No. 157, LEADENHALL STREET.

1852.

PRICE SIXTEEN SHILLINGS BOUND.

Verificación en una tabla de *versed sines*  
de los valores encontrados con el *Omnimetre*

| TABLE XXXVI.                              |        |                   |          |        |                   |          |        |                   |          |        |                   |          | 233       |
|-------------------------------------------|--------|-------------------|----------|--------|-------------------|----------|--------|-------------------|----------|--------|-------------------|----------|-----------|
| Natural <i>Versed</i> and Suversed Sines. |        |                   |          |        |                   |          |        |                   |          |        |                   |          |           |
| 1<br>"<br>Vers.                           | 4°     |                   |          | 5°     |                   |          | 6°     |                   |          | 7°     |                   |          | "<br>Sum. |
|                                           | Versed | Parts<br>for<br>" | Suversa. | Versed | Parts<br>for<br>" | Suversa. | Versed | Parts<br>for<br>" | Suversa. | Versed | Parts<br>for<br>" | Suversa. |           |
| 0                                         | 002436 | 0                 | 1.997561 | 003805 | 0                 | 1.996195 | 005478 | 0                 | 1.994522 | 007454 | 0                 | 1.992546 | 60        |
| 1                                         | 02456  | 0                 | 97544    | 03831  | 0                 | 96169    | 05509  | 1                 | 94491    | 07489  | 1                 | 92511    | 59        |
| 2                                         | 02477  | 1                 | 97523    | 03856  | 1                 | 96144    | 05539  | 1                 | 94461    | 07525  | 1                 | 92475    | 58        |
| 3                                         | 02497  | 1                 | 97503    | 03882  | 1                 | 96118    | 05570  | 2                 | 94430    | 07561  | 2                 | 92439    | 57        |
| 4                                         | 02518  | 1                 | 97482    | 03907  | 2                 | 96093    | 05600  | 2                 | 94400    | 07596  | 2                 | 92404    | 56        |
| 5                                         | 02538  | 2                 | 97462    | 03933  | 2                 | 96067    | 05631  | 3                 | 94369    | 07632  | 3                 | 92368    | 55        |
| 6                                         | 02559  | 2                 | 97441    | 03959  | 3                 | 96041    | 05662  | 3                 | 94338    | 07668  | 4                 | 92332    | 54        |
| 7                                         | 02580  | 3                 | 97420    | 03985  | 3                 | 96015    | 05693  | 4                 | 94307    | 07704  | 4                 | 92296    | 53        |
| 8                                         | 02601  | 3                 | 97399    | 04011  | 3                 | 95989    | 05724  | 4                 | 94276    | 07740  | 5                 | 92260    | 52        |
| 9                                         | 02622  | 3                 | 97378    | 04037  | 4                 | 95963    | 05755  | 5                 | 94245    | 07776  | 6                 | 92224    | 51        |
| 10                                        | 02643  | 4                 | 97357    | 04063  | 4                 | 95937    | 05786  | 5                 | 94214    | 07813  | 6                 | 92187    | 50        |
| 11                                        | 002664 | 4                 | 1.997336 | 004089 | 5                 | 1.995911 | 005818 | 6                 | 1.994182 | 007849 | 7                 | 1.992151 | 49        |
| 12                                        | 02685  | 4                 | 97315    | 04116  | 5                 | 95884    | 05849  | 6                 | 94151    | 07885  | 7                 | 92115    | 48        |
| 13                                        | 02707  | 5                 | 97293    | 04142  | 6                 | 95858    | 05880  | 7                 | 94120    | 07922  | 8                 | 92078    | 47        |
| 14                                        | 02728  | 5                 | 97272    | 04168  | 6                 | 95832    | 05912  | 7                 | 94088    | 07958  | 9                 | 92042    | 46        |
| 15                                        | 02750  | 5                 | 97250    | 04195  | 7                 | 95805    | 05944  | 8                 | 94056    | 07995  | 9                 | 92005    | 45        |
| 16                                        | 02771  | 6                 | 97229    | 04222  | 7                 | 95778    | 05975  | 8                 | 94025    | 08032  | 10                | 91968    | 44        |
| 17                                        | 02793  | 6                 | 97207    | 04248  | 7                 | 95752    | 06007  | 9                 | 93993    | 08069  | 10                | 91931    | 43        |
| 18                                        | 02815  | 6                 | 97185    | 04275  | 8                 | 95725    | 06039  | 9                 | 93961    | 08106  | 11                | 91894    | 42        |
| 19                                        | 02837  | 7                 | 97163    | 04302  | 8                 | 95698    | 06071  | 10                | 93929    | 08143  | 12                | 91857    | 41        |
| 20                                        | 02859  | 7                 | 97141    | 04329  | 9                 | 95671    | 06103  | 10                | 93897    | 08180  | 12                | 91820    | 40        |

versed sines de 5° 8' = 0.04011

TABLE XXXVI.  
Natural Versed and Suversed Sines.

| Versed. | 16°     |             |          | Versed. | 17°     |             |          | Versed. | 18°      |             |          | Versed.  | 19°     |             |          | Sum. |
|---------|---------|-------------|----------|---------|---------|-------------|----------|---------|----------|-------------|----------|----------|---------|-------------|----------|------|
|         | Versed. | Parts for " | Suversa. |         | Versed. | Parts for " | Suversa. |         | Versed.  | Parts for " | Suversa. |          | Versed. | Parts for " | Suversa. |      |
| 0       | 038738  | 0           | 1.961262 | 043695  | 0       | 1.956305    | 048943   | 0       | 1.951057 | 054481      | 0        | 1.945519 | 060     |             |          | 60   |
| 1       | 38818   | 1           | 61182    | 43780   | 1       | 50220       | 49033    | 2       | 50967    | 54376       | 2        | 45424    | 50      |             |          | 50   |
| 2       | 38899   | 3           | 61101    | 43865   | 3       | 56135       | 49123    | 3       | 50877    | 54671       | 3        | 45320    | 58      |             |          | 58   |
| 3       | 38079   | 4           | 61021    | 43951   | 4       | 56049       | 49213    | 5       | 50787    | 54766       | 5        | 45234    | 57      |             |          | 57   |
| 4       | 39060   | 5           | 60940    | 44036   | 6       | 55964       | 49304    | 6       | 50696    | 54861       | 6        | 45139    | 56      |             |          | 56   |
| 5       | 39140   | 7           | 60860    | 44121   | 7       | 55879       | 49394    | 8       | 50606    | 54956       | 8        | 45044    | 55      |             |          | 55   |
| 6       | 39221   | 8           | 60779    | 44207   | 9       | 55793       | 49484    | 9       | 50516    | 55051       | 10       | 44949    | 54      |             |          | 54   |
| 7       | 39302   | 9           | 60698    | 44293   | 10      | 55707       | 49575    | 11      | 50425    | 55146       | 11       | 44854    | 53      |             |          | 53   |
| 8       | 39382   | 11          | 60618    | 44378   | 11      | 55622       | 49665    | 12      | 50335    | 55242       | 12       |          | 52      |             |          | 52   |
| 9       | 39463   | 12          | 60537    | 44464   | 13      | 55536       | 49756    | 14      | 50244    | 55337       | 14       |          |         |             |          |      |
| 10      | 39544   | 14          | 60456    | 44550   | 14      | 55450       | 49846    | 15      | 50154    | 55432       | 15       |          |         |             |          |      |
| 11      | 039625  | 15          | 1.960375 | 044636  | 16      | 1.955364    | 049037   | 17      | 1.950063 | 055528      | 17       |          |         |             |          |      |
| 12      | 39706   | 16          | 60294    | 44722   | 17      | 55278       | 50028    | 18      | 49972    | 55624       | 18       |          |         |             |          |      |
| 13      | 39787   | 18          | 60213    | 44808   | 19      | 55192       | 50119    | 20      | 49881    | 55719       | 20       |          |         |             |          |      |
| 14      | 39869   | 19          | 60131    | 44894   | 20      | 55106       | 50210    | 21      | 49790    | 55815       | 21       |          |         |             |          |      |
| 15      | 39950   | 20          | 60050    | 44980   | 22      | 55020       | 50301    | 23      | 49699    | 55911       | 23       |          |         |             |          |      |
| 16      | 40032   | 22          | 59968    | 45066   | 23      | 54934       | 50392    | 24      | 49608    | 56007       | 24       |          |         |             |          |      |
| 17      | 40113   | 23          | 59887    | 45153   | 24      | 54847       | 50483    | 26      | 49517    | 56103       | 26       |          |         |             |          |      |
| 18      | 40195   | 24          | 59805    | 45239   | 26      | 54761       | 50574    | 27      | 49426    | 56199       | 27       |          |         |             |          |      |
| 19      | 40276   | 26          | 59724    | 45326   | 27      | 54674       | 50666    | 29      | 49334    | 56295       | 29       |          |         |             |          |      |
| 20      | 40358   | 27          | 59642    | 45412   | 29      | 54588       | 50757    | 30      | 49243    | 56391       | 30       |          |         |             |          |      |
| 21      | 040440  | 28          | 1.959560 | 045499  | 30      | 1.954501    | 050849   | 32      | 1.949151 | 056488      | 32       |          |         |             |          |      |
| 22      | 40522   | 30          | 59478    | 45586   | 32      | 54414       | 50940    | 33      | 49060    | 56584       | 33       |          |         |             |          |      |
| 23      | 40604   | 31          | 59396    | 45673   | 33      | 54327       | 51032    | 35      | 48968    | 56681       | 35       |          |         |             |          |      |
| 24      | 40686   | 32          | 59314    | 45760   | 35      | 54240       | 51124    | 36      | 48876    | 56777       | 36       |          |         |             |          |      |

versed sines de 16° 16' = 0.040032

Verificación en una tabla de versed sines  
de los valores encontrados con el Omnimetre

Natural Versed and Suversed Sines.

| Versed. | 24°     |             |          | Versed. | 25°     |             |          | Versed. | 26°      |             |          | Versed.  | 27°     |             |          | Sum. |
|---------|---------|-------------|----------|---------|---------|-------------|----------|---------|----------|-------------|----------|----------|---------|-------------|----------|------|
|         | Versed. | Parts for " | Suversa. |         | Versed. | Parts for " | Suversa. |         | Versed.  | Parts for " | Suversa. |          | Versed. | Parts for " | Suversa. |      |
| 0       | 086454  | 0           | 1.913546 | 093602  | 0       | 1.906308    | 101206   | 0       | 1.898794 | 108903      | 0        | 1.891007 | 60      |             |          | 60   |
| 1       | 86573   | 2           | 13427    | 93815   | 2       | 06185       | 01333    | 2       | 98667    | 09120       | 2        | 90874    | 59      |             |          | 59   |
| 2       | 86691   | 4           | 13309    | 93938   | 4       | 06062       | 01461    | 4       | 98539    | 09258       | 4        | 90742    | 58      |             |          | 58   |
| 3       | 86810   | 6           | 13190    | 94061   | 6       | 05939       | 01589    | 6       | 98411    | 09390       | 6        | 90610    | 57      |             |          | 57   |
| 4       | 86928   | 8           | 13072    | 94185   | 8       | 05815       | 01717    | 8       | 98283    | 09522       | 8        | 90478    | 56      |             |          | 56   |
| 5       | 87047   | 10          | 12953    | 94308   | 10      | 05692       | 01844    | 11      | 98156    | 09655       | 11       | 90345    | 55      |             |          | 55   |
| 6       | 87166   | 12          | 12834    | 94431   | 12      | 05569       | 01972    | 13      | 98028    | 09787       | 13       | 90213    | 54      |             |          | 54   |
| 7       | 87285   | 14          | 12715    | 94555   | 14      | 05445       | 02100    | 15      | 97900    | 09920       | 15       | 90080    | 53      |             |          | 53   |
| 8       | 87403   | 16          | 12597    | 94678   | 16      | 05322       | 02228    | 17      | 97772    | 10052       | 17       | 89948    | 52      |             |          | 52   |
| 9       | 87522   | 18          | 12478    | 94802   | 18      | 05198       | 02357    | 19      | 97643    | 10185       | 19       | 89815    | 51      |             |          | 51   |
| 10      | 87642   | 20          | 12358    | 94925   | 21      | 05075       | 02485    | 21      | 97515    | 10318       | 21       | 89682    | 50      |             |          | 50   |
| 11      | 087761  | 22          | 1.912239 | 095049  | 23      | 1.904951    | 102613   | 23      | 1.897387 | 110451      | 23       | 1.889549 | 49      |             |          | 49   |

versed sines de 24° = 0.086454

|    |        |     |          |        |     |          |        |     |          |        |     |          |    |
|----|--------|-----|----------|--------|-----|----------|--------|-----|----------|--------|-----|----------|----|
| 45 | 91857  | 90  | 08143    | 99302  | 95  | 00698    | 07021  | 97  | 92979    | 15012  | 101 | 84988    | 15 |
| 46 | 91979  | 92  | 08021    | 99428  | 97  | 00572    | 07152  | 100 | 92848    | 15148  | 103 | 84852    | 14 |
| 47 | 92100  | 94  | 07900    | 99555  | 99  | 00445    | 07283  | 102 | 92717    | 15283  | 105 | 84717    | 13 |
| 48 | 92222  | 96  | 07778    | 99681  | 101 | 00319    | 07414  | 104 | 92586    | 15419  | 107 | 84581    | 12 |
| 49 | 92345  | 98  | 07655    | 99808  | 103 | 00192    | 07545  | 106 | 92455    | 15555  | 110 | 84445    | 11 |
| 50 | 92467  | 100 | 07533    | 99935  | 105 | 1.90065  | 07677  | 108 | 92323    | 15690  | 112 | 84310    | 10 |
| 51 | 092589 | 102 | 1.907411 | 100061 | 107 | 1.899939 | 107808 | 111 | 1.892192 | 115826 | 114 | 1.884174 | 9  |
| 52 | 092711 | 104 | 07980    | 00188  | 109 | 09819    | 07939  | 113 | 09061    | 15869  | 116 | 84038    | 8  |

versed sines = 1 para 25° 51'

## Significado de la escala Gunter V.S

**A line of Versed Sines, marked V. S. This line, when compared with that of sines, &c. is useful in finding the sun's true azimuth, or the apparent time, the sun's altitude, declination, and the latitude of the place, being given.**

Ron Manleys dice lo siguiente sobre la escala V.S. :

A pair of adjacent scales marked SIN and V.SIN. In navigation use is sometimes made of Versines (or Versed sine), such that Versine ( $q$ ) =  $2 \sin^2(q/2)$ , or Haversine such that Haversine ( $q$ ) =  $\sin^2(q/2)$ .

The pairs of values of this scale are arranged such that the sine of the angles marked SIN have the same values as  $1 - \text{Haversine}$ .

For example: Haversine ( $90^\circ$ ) =  $\sin^2(45^\circ)$  = 0.7072 .

$$1 - 0.7072^2 = 0.5$$

$$\sin^{-1}(0.5) = 30^\circ$$

As can be seen the  $90^\circ$  on the V.SIN line is adjacent the  $30^\circ$  on the SIN line

<http://www.sliderules.info/collection/specialised/9948-navigation.htm>

Otto van Poelje dice al respecto :

Logarithmic scales - NUM, SIN, TAN, S \* R, T \* R, V \* S

...

The scale title V \* S means *versed sines* but it does not reflect our current versine which equals  $(1 - \cos)$ .

It actually represents, in modern terminology, the logarithm of  $(1 - \text{haversine})$ , or  $\frac{1}{2} (1 + \cos)$ .

The haversine function (half-versed-sine) was introduced for computational reasons in the formula which calculates the angular distance between two arbitrary points on the globe. This formula could be calculated between the NUM, the SIN and the V \* S scales on the Gunter rule.

***Journal of the Oughtred Society Vol. 13, No. 1, Spring Issue 2004***